Mat-2.177 Seminar on case studies in operations research

Decision-Making support system for flood control

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1 Introduction

1.1 Background

1.1.1 Client - EIA

Environmental Impact Assessment Centre of Finland Ltd. (EIA) is an independent research company. The main aim of the company is to apply state of the art mathematical models for practical demands, and to maintain the validity of models with their continuous development and critical evaluation against field observations. EIA models have been developed for watersheds, rivers, lakes, coastal and sea areas and atmosphere.

This project concerned watershed management and river flood risk analysis. Risk analyses of floods and decision-making support systems for watershed management have become even more important as hydroelectric power plants have become more common.

1.1.2 Case - Yangtze River flood modeling

Yangtze River in China is one largest in the world and some 400 million people live in the area watered by it. There are lots of dams and hydroelectric power plants along the Yangtze. The flow data has been generated for six rivers and for a period of 50 years.

The decision-making situation has two contradicting goals. For maximal productivity of a power plant, the surface of a basin should be as high as possible. The safest situation conversely is that the surface is as low as possible.

1.1.3 Assignment and objectives

EIA formulated the following tasks to the project group:

- 1. Determine the probability that certain river flows (case Yangtze) exceed maximum tolerance given in 50, 100 and 200 years, provided that long history of the flows is given.
- 2. Determine optimal actions concerning basin and reserve area usage at every moment with the condition that the risk level is to be less than 0.001. At the strating point all dam and river areas are at their minimum level. Future flows are not known at the decision point.
- 3. Design a dynamic method or application to produce optimal actions, when costs and risk levels are known.
- 4. Apply this method to case Yangtze.

EIA delivered us flow data of 6 tributary river of Yangtze, measured daily over 50 years. Also the cost levels of floods, capacity of basins and the delays of fulfillments of the reserve areas were known. The main goal in the project was the design of the decision-making method (mentioned above in 3. task) to aid in taking optimal actions.

1.1.4 Structure of the project

The project can be seen to have consisted of two main parts. The first part was to analyze the flow data given. The first idea was to identify the SARIMA-processes of flows and to estimate the parameters. This would probably be the most suitable approach, but because the assignment was also to calculate probabilities for long term events, we decided not to use time series analysis.

The bigger or at least more relevant part of this project was to analyze the decision-making situation. The goal was to come up with some method, which determines what actions to take under certain conditions.

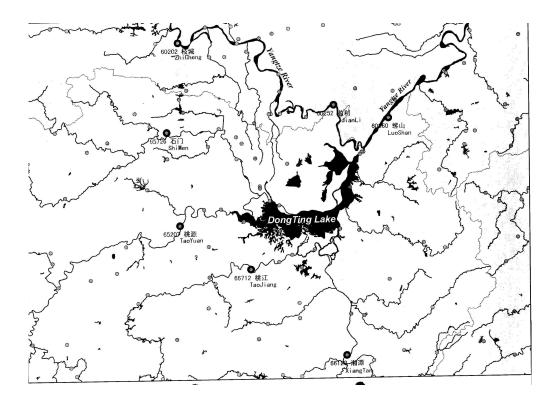


Figure 1: The Yangtze river and the surrounding areas.

1.1.5 Project excecution

The greatest problem in achieving the objectives of the project was that the group worked on a virtual basis. Each member lived in different town and the group communicated mainly through e-mail. This hindered the effectiveness of communication, reduced the exchange of ideas and complicated the execution of the project.

Despite the careful planning of actions in the project the risks in many ways came true. Virtual meetings between team members did not compensate the need for real meetings which all could take place. This hindered in advancing in the project. Afterwards, also the management of the team could have been more dispersed to all the team members.

Since there was only one person really responsable of designing the method to be used in the project case, this would have facilitated the project as well. Much time was also used for clarifying the assignment as well. This could have been easily bypassed by more accurate project information in the beginning of project from EIA.

The co-operation it self worked out fine, both to EIA and within the team. Team spirit was good and open for discussions to solve problems of all kinds. However, there is still much learning to do in project work. Especially the schedule must be carefully followed to able to attain results within the time limits.

1.2 Literature review

The project group carried out a literary review to be aware of the theoretical background of the assignment. When the project was initiated, no one in the project group was familiar with flood modeling or environmental risk analysis. The group discovered that the amount of applicable previous studies on the subject was to some extent limited. Therefore the process of designing the decision-making system was quite intuitive in nature. The most relevant piece of research for designing the decision-making system is presented below.

These studies with different mathematical methods have been done based on different kinds of time series. One aspect is to measure daily rainfall in certain area. More common approach ist to monitor the streamflow, as W. Boughton et al [4] has demonstrated.

Analysing rainfall time series, or any other data than flows, requires a lot more complex analysis, since rainfall and river flows can be rather uncorrelated. In this light, the use of river flow data has a straightforward basis.

Zhang et al (2002) presented an application of an improved linear storage

routing model for the estimation of large floods. They emphasized that while conceptual storage routing models have been developed for the same purpose, one of their key components had been the assumed non-linear storage-discharge relationship. In addition, Australian Rainfall and Runoff (Institution of Engineers, 1987) had actually recommended this relationship to be used in the estimation of large floods.

However, also models with other kinds of storage-discharge relationships have been developed. The relationship has been modeled e.g. as asymptotically linear, non-linear with an intercept and as linear. As to which relationship best models the phenomenon, it has been shown that catchments tend to operate as linear systems in larger floods (Zhang, 2001).

In addition, the project group studied articles and literature on flood forecasting (Toth et al., 1998; Strupczewski et al., 2000) and environmental risk analysis in general (Lerche & Paleologos, 2001).

The theoretical approach of this study shared a similar line of thought with the work of Zhang. The theoretical approach will be presented in more detail in subsequent chapters.

1.3 Structure of the report

After this introductory chapter, the decision-making situation will be described in the next chapter. In the third chapter, our approach will be presented in more detail. The chapter also covers the restrictions of our solution and the formulation of the problem. The fourth chapter consists of a discussion of the contribution of the decision-making system. Finally, in the fifth chapter the decision-making system is applied to the case of Yangtze River.

2 Decision situation

The decision situation of systems with many tributary rivers can be divided into parts and each river can be treated independently. In the case of tributary rivers the net effect can be modeled by analysing the sum flows. Thus, every system can be divided into smaller subproblems which can be analyzed as a one basin systems. In future we will concentrate in these so called "one-basin systems".

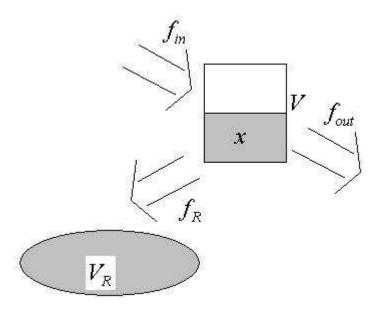


Figure 2: Schematic diagram of a one-basin system. In the middle there is the basin and in the lower left corner the reservoir area.

Assume the basin volume to be V. In the decision situation the current water level of the basin is known. The electricity produced depends linearly on the water level. Assume that the gain of maximum electricity production to be M. There are also an option of using the reservoir area. This involves a non-recurring cost of C. Assume that the volume of the reservoir area is V_R and it fills with constant speed until time T_R (then it's full). If the basin floods, there will be a fine (penalty) of F. The flow put into the river from the basin must not exceed K.

3 Our approach

The data given by EIA of daily measurements made of flow rates from main and tributary rivers from last 50 years leads to use the statistical means in analysing the flood risks. Generally, flow data is typically collected in some form, so our approach presented below is fairly applicable.

In analyzing the river floods the main intrest is to determine the floods probabilities corresponding the decisions made about the basin surface height. We think it is natural to assume that some kind of distributions of the river flows can be estimated. This is also a natural way of approaching the probabilities mentioned above.

This probabilistic approach is easily applied to different kinds of systems, but this generality of course requires simplification of systems.

We approach the decision-making in a following sense: decisions are made discretely at (constant) Δt time intervals. Δt should be chosen small enough, so that this discretation isn't too robust. If $\Delta t \to 0$ the decision-making is in a sense continuous.

3.1 Problem formulation

Naturally the optimization task is to maximize the financial profit of the hydroelectric power plant. If the reservoir usage cost C and flood penalty F are rather small the optimal solution would result from keeping the water level as high as possible throughout the year and accept either the reservoir usage cost C or the flood fine F. To be able to take into account also the humane risks, the risk level itself should also be controlled in some way.

Thus, for humane and political causes it is necessary to add a constraint to keep the risk level low enough. We use a very intuitive constraint, the risk level of the flood must stay below 0.001. Probability P(flood isn't avoidable) is quite hard to calculate, because it consists of the events that flood isn't avoidable and occurs at latest at time t_i , i = 1...

This problem can be set aside, because the probabilities that the flood occures much later than now are very small. Thus, the risk level can be approximated by discarding these probabilities.

Denote the degree of fullness of the basin at the time t_n by x_n . Formulating our approach into an optimization problem, at time t_n the decision problem is

$$\max \ M * \min(1, E[x_{n+1}]) - (1 - y_{1,n-1}) * y_{1,n} * C - y_{2,n} * F$$
s.t. $P(x_{n+1} > 1 \text{ or } x_{n+2} > 1) \le 0.001$ (1)

where,

$$x_{n+1} = x_n + (V_{in,n} - V_{out,n})/V, x_n \ge 0$$

 $V_{in,n}$ is the volume of the water flown into the basin from the river. $V_{in,n}$ is a random variable and thus x_{n+1} is also a random variable.

 $V_{out,n}$ is the volume of the water passed through the dam or put into reservoir area. $V_{out,n}$ is a direct consequence of our decisions.

 $y_{1,n}$ is the indicator of using the reservoir area, and a decision variable $y_{2,n}$ is the indicator of flood.

 $y_{1,n}, y_{2,n}$ and $V_{out,n}$ can be expressed in

$$y_{1,n} = \begin{cases} 1 \text{ ,if reservoir area is used} \\ 0 \text{ ,otherwise} \end{cases}$$
 $y_{2,n} = \begin{cases} 1 \text{ ,if } x_{n+1} > 1 \\ 0 \text{ ,otherwise} \end{cases}$ $V_{out,n} = f_{out,n} + y_{1,n} * \frac{V_R}{T_R}$

and $f_{out,n}$ is of course a decision variable, $0 \le f_{out,n} \le K$.

3.2 Restrictions

The most obvious restriction of this approach is that some kind of estimated distribution of future river flows are assumed to be available. As already mentioned earlier, this data is although often collected and this restriction isn't at all limiting.

The decision is made discretely and this might be a restriction to some dynamic models. Although the qualitative behaviour of the model should be sufficiently dynamic, when Δt is chosen small enough.

All in all, this approach is in its plainess quite flexible and very applicable to different situations because the main idea is very general.

4 Discussion

This method that has been generated is very straightforward and applicable. There are certain weaknesses or disadvantages concerning the model, and these will be analysed in this section.

4.1 The dynamics of the model

When collecting the data it is important to be sure that the measurements will give an representative sample of the flow or water level behaviour. If the water level is fluctuating all the time, it is possible that the flow maximum will occur between the measurements.

For example if the data is measured daily at noon, but the flow fluctuates throughout the day, the measurements won't give a proper view of the situation. It is also possible that the data isn't representative in the sense that it doesn't show out longer-term effects, e.g. greenhouse effect.

Choosing a good time interval for measurements requires knowledge of the qualitative behaviour of the flood. This time interval is also very closely related to the Δt in the decision-making method. Both intervals should be chosen so that the flows wouldn't fluctuate too much during this interval. It would naturally be suitable to choose this measurement and decision time interval to same Δt .

Analytically it is hard to determine, how small Δt should be for the decision-making to "work". Although, as will be seen later in the case test runs, the

river flows maybe quite static and also a big Δt can handle the situation. In the this case example the values for $\Delta t = 1$ day and $\Delta t = 2$ days were tested. When determining a suitable time interval, one should always think how rapidly the river flows change and choose a value for Δt accordingly.

4.2 Estimating the flow distributions

In the method the most binding assumption is that the future flow distributions can be estimated. Even if the estimating can be done, there is uncertainty in the estimates. For example, if the distribution is parametric, the estimated parameter(s) can be biased. This problem dealing with the estimation biases isn't analyzed in this paper, nut being aware of this risk factor can be crucial.

4.3 Calculating the risk levels

The risk level for flood to occur is very hard to calculate, because the inevitable flood can theoretically realize also after a very long period of time. To ease the calculation these probabilities can be cut off and the risk at time t_n can be thought to consist of the events 'The flood occurs at time t_k ', $n \le k \le n+m$

These "cut-offs" ease the calculation rapidly, but the disadvantages aren't that big at all. These "tail probabilities" are normally very small.

5 Case Yangtze

5.1 Data analysis

The data was classified both to daily (to 365 cases) and to monthly classes. Little surprisingly, none the samples could be identified to be produced by a normal distribution. Instead, the histograms referred to χ^2 -distributions. This

interesting fact is though as such irrelevant to this decision-making method and no statistical testing was made for this hypothesis. The statistics of sum flow and flow 2 are represented in appendices.

Let denote the events

 A_i ='SUMFLOW doesn't exceed 78500 m^3/s in month i' and B_i ='FLOW2 doesn't exceed 5500 m^3/s in month i.' i = 1, ..., 12 and $P(A_i) =: p_i$ and $P(B_i) = q_i$. These probabilities can be estimated by histogram method (presented e.g. by Clemen [5]). For example

$$p_1 = 1, q_7 = \left(\frac{1538}{1550}\right)^{31} = 0.78589, p_6 = \left(\frac{1491}{1500}\right)^{30} = 0.83482$$

Now, probabilities

P(SUMFLOW doesn't exceed 78500 m^3/s in N years)

$$= \left(\Pi_{i=1}^{12} p_i^N\right) = (0.88671 * 0.88671 * 0.69621)^N$$

P(FLOW2 doesn't exceed 5500 m^3/s in N years)

$$= \left(\Pi_{i=1}^{12} q_i^N\right) = (0.88671 * 0.94171 * 0.80189)^N$$

Both probabilities are smaller than 10^{-8} , when $N \geq 50$. The fact that these probabilities are very very small isn't that surprising, because we are dealing with very long periods of time. It would, indeed be unexpected that during a 50 year period, there were no floods.

This approach has although a remarkable theoretical weakness: it doesn't take into account dependencies between daily flows. One could for example imagine that floods last for at least some days. In general, assumption of independent daily flows is hardly true and better approach would be to examine the monthly maximum flows.

This kind of aspect wouldn't though be applicable for the decision-making mehtod constructed in chapter 3.1. We also supposed that the error caused by this assumption is reasonable and on the other hand it allows the usage of the decision-making method.

5.2 Method demonstration

Now let's demonstrate the decision-making method. The method is applied to one of the tributary rivers of Yangtze. The data is given by EIA and the date is July 10th, 1984. The parameters are as follows:

The basin volume $V=1.5*10^9m^3$ The gain from electricity production $M=10^6\mathrm{Eur}$ Volume of the reservoir area $V_R=0.3*10^9m^3$ Cost from using the reservoir area $C=50*10^6\mathrm{Eur}$ The time it takes to full the reservoir area $T_R=3$ days The fine from flood $F=500*10^6\mathrm{Eur}$ The maximum flow in the river $K=5500m^3/s$

Since the data has been given in daily intervals, logical idea is to choose the interval also for the model to be the same, i.e. $\Delta t = 1$ day. Choosing a shorted period would lead to new problemes and it would require further assumptions of the water level change and also the generation of the data for these moments as well. For the sake of researching the effect of Δt same situation is demonstrated with a run of $\Delta t = 2$ days.

At each decision state the problem (1) is solved. It is important to notice that in calculating the risk level, the approximated density function of the $f_{in,n+1}$ is utilized.

The results are rather good and both values for Δt lead to quite similar behaviour. The run with $\Delta t = 2$ days is probably a bit more careful. This is also very intuitive, because the variance of $f_{in,n+1}$ is four times as big as with $\Delta t = 1$ day, while the expected value is just twice as big.

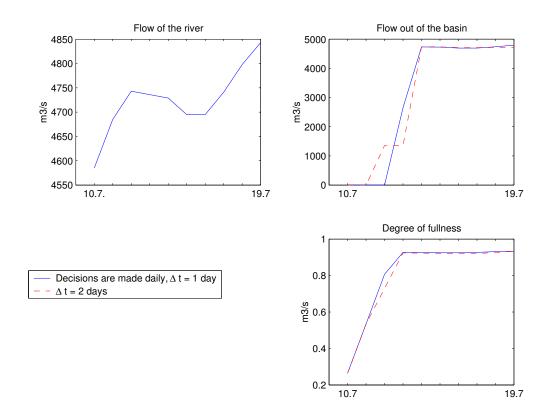


Figure 3: Results of a test run

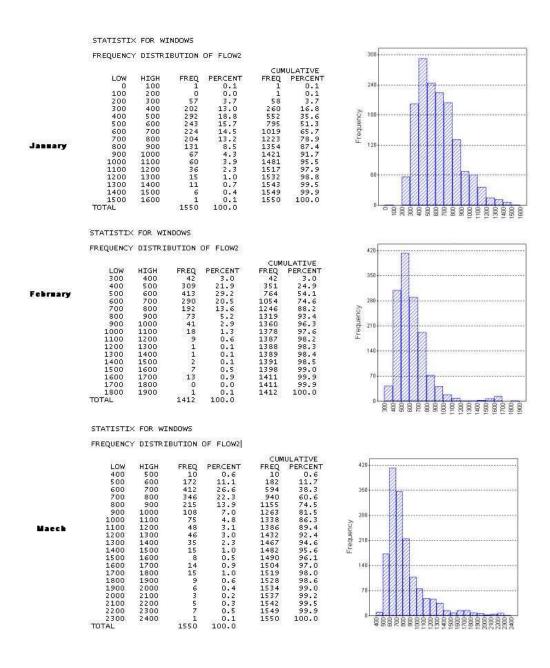
In both runs the degree of fullness of the basin first grow from 0 to over 0.9 and quickly stabilizes little above 0.9. This method seems to handle this situation fairly well.

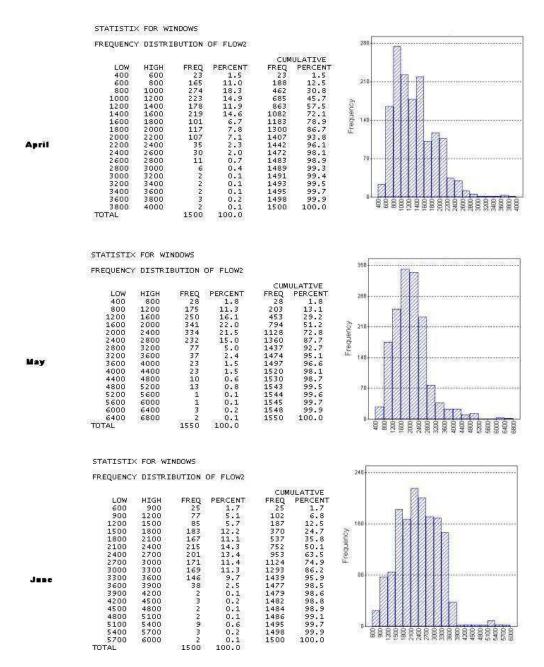
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Appendices

Flow 2 and SUMFLOW data sorted by month.





	July					\$TATISTIX	FOR WI	NDOWS	August		
STATISTI	EX FOR W	INDOWS				FREQUENCY	DISTRI	BUTION	OF FLOW2		
FREQUENC 600 900 1200 2100 2100 3000 3300 3600 3900 4200 4500 4500 5100 5700 TOTAL	HIGH 900 1200 1200 1200 2400 3000 3300 3300 4200 4500 4500 5700 6000	FREQ 8 8 6 4 4 91 1100 192 239 198 148 161 966 37 63 45 50 23 22 21 3 4 1550	OF FLOW2 PERCENT 0.5 0.4 2.8 5.9 7.1 12.4 15.4 12.8 9.5 10.4 6.2 5.6 4.1 2.9 1.5 1.4 0.8 0.3 100.0	CUI FREQ 8 144 58 149 259 451 6900 888 1197 1297 1293 1380 1443 1513 1533 1546 1550	MULATIVE PERCENT 0.5 0.9 3.7 9.6 16.7 29.1 44.5 57.3 86.8 77.2 83.1 96.0 97.5 98.9 99.7	LOW 600 800 1000 1000 1200 1400 2000 2400 2400 3600 3600 3600 4200 4400 4600 4800 TOTAL	HIGH 800 1200 1200 1400 1600 2000 2200 22400 22800 33000 3400 3400 3400 4400 4400 4400	FREQ 3 3 3 3 2 64 82 2 110 164 159 174 188 175 115 92 27 22 27 32 25 18 10 10 10 10 10 10 10 10 10 10	PERCENT 0.2 0.2 0.2 1.3 4.1 5.3 7.1 10.6 10.3 11.2 12.1 11.3 7.4 5.9 4.6 1.7 2.1 1.6 0.8 0.0 0.8 0.0 0.1	CUM FREQ 3 3 6 9 29 93 175 285 449 608 782 970 1145 1260 1352 1424 1451 1483 1508 1526 1536 1536 1549 1550	ULATIVE PERCENT 0.2 0.4 0.6 1.9 6.0 11.3 18.4 29.0 39.2 50.5 62.6 73.9 81.3 87.2 91.9 93.6 95.7 99.9 100.0
\$ ptatistix	Septem l						Octo	ber			
FREQUENCY	DISTRIE	BUTION O	F FLOW2			STATISTIX	FOR WI	NDOWS			
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 statistix	FOR WI										
FREQUENCY	DISTRI	BUTION C	OF FLOW2	9322483	JLATIVE	STATISTIX	Dece FOR WIN				
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STATISTI	× FOR W	INDOWS	January								
FREQUENC	Y DISTRI	BUTION	OF SUMFLOW				Febr	rary			
LOW	HIGH	FREQ	PERCENT	CUM FREQ	ULATIVE PERCENT	STATIST:	IX FOR SU	MFLOW			
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10000	11000 12000	200 158	12.9	1083	69.9 80.1	7000 8000	8000 9000	211 357	14.9 25.3	289 646	20.5 45.8
12000 13000	13000 14000	87 47	5.6 3.0	1328	85.7 88.7	9000 10000	10000	240 172	17.0	886 1058	62.7 74.9
14000	15000	45	2.9	1420	91.6	11000 12000	12000 13000	111	7.9 4.5	1169 1233	82.8 87.3
15000 16000	16000 17000	55 31	3.5 2.0	1475 1506	95.2 97.2	13000 14000	14000 15000	55 34	3.9	1288	91.2 93.6
17000 18000 19000	18000 19000 20000	16 6 5	1.0 0.4	1522	98.2 98.6 98.9	15000 16000	16000 17000	23 18	1.6	1345	95.3 96.5
20000	21000	5	0.3	1533	99.2 99.5	17000 18000	18000 19000	8 14	0.6	1371 1385	97.1 98.1
21000	23000	3	0.3	1543 1546 1548	99.7	19000 20000	20000	17	1.2	1402 1410	99.3
23000	24000 25000	2 0 1	0.1	1548	99.9 99.9	21000	22000	1	0.1	1411	99.9 100.0
25000 26000	26000	0	0.1	1549 1549	99.9 99.9	TOTAL	23000	1412	100.0	1412	100.0
27000 TOTAL	28000	1 1550	0.1 100.0	1550	100.0						
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9000 10000	10000 11000	12 <i>7</i> 311	8.2 20.1	159 470	10.3	12000 14000	14000 16000 18000	155 171	10.3	253 424	16.9 28.3
11000 12000	12000	259 265	16.7 17.1	729 994	47.0 64.1	16000 18000	20000	159 137 155	10.6 9.1	583 720	38.9 48.0
13000 14000	14000 15000	168 85	10.8 5.5	1162 1247	75.0 80.5	20000 22000	24000	115	7.7	875 990 1086	58.3 66.0 72.4
15000 16000	16000 17000	62 39	4.0	1309 1348	84.5 87.0	24000 26000 28000	26000 28000 30000	96 97 72	6.4 6.5 4.8	1183	78.9 83.7
17000 18000	18000 19000	24 26	1.5	1372 1398	88.5 90.2	30000 32000	32000 34000	75 56	5.0	1255 1330	88.7 92.4
19000 20000	20000 21000	34 25	1.6	1432 1457	92.4 94.0	34000 36000	36000 38000	21 43	3.7 1.4 2.9	1386 1407 1450	93.8 96.7
21000 22000	22000 23000	24 14	1.5 0.9	1481 1495	95.5 96.5	38000 40000	40000 42000	21 10	1.4	1471 1481	98.1 98.7
23000 24000	24000 25000	15 13	1.0 0.8	1510 1523	97.4 98.3	42000 44000	44000 46000	6	0.4	1487	99.1 99.4
25000 26000	26000 27000	13	0.5	1531 1544	98.8 99.6	46000 48000	48000 50000	3 4	0.2	1494 1498	99.6
27000 28000	28000 29000	2	0.1	1546 1549	99.7 99.9	50000 52000	52000 54000	i 0	0.1	1499 1499	99.9 99.9
29000 TOTAL	30000	1 1550	0.1 100.0	1550	100.0	54000 TOTAL	56000	1 1500	0.1 100.0	1500	100.0
BTATIST:				May		S TATISTI	× FOR WI	NDOWS	Jane	ı	
PREQUENC	. 1 DISTR	TROUTON	OF SUMFLOY		MULATIVE	FREQUENC	Y DISTRI	BUTION (OF SUMFLOW		
LOW 8000	HIGH 12000	FREQ 27	PERCENT 1.7	FREQ 27	PERCENT 1.7	LOW	HIGH		PERCENT	FREQ	ULATIVE PERCENT
12000 16000	16000	70 93	4.5 6.0	97 190	6.3	8000 12000	12000 16000	6 24	0.4 1.6	30 30	0.4
20000	24000 28000	151 227	9.7 14.6	341 568	12.3 22.0 36.6	16000 20000	20000 24000	23 89	1.5	53 142	3.5 9.5
28000 32000	32000 36000	243	15.7 15.6	811 1053	52.3 67.9	24000 28000	32000	123 171	8.2 11.4	265 436	17.7 29.1
36000 40000	40000	231 106	14.9	1284 1390	82.8	32000 36000	36000 40000	207 171	13.8 11.4	643 814	42.9 54.3
44000 48000	48000 52000	45 32	6.8 2.9 2.1	1435 1467	89.7 92.6 94.6	40000 44000	44000 48000	136 228	9.1 15.2	950 1178	63.3 78.5
52000 56000	56000 60000	11 27	2.1 0.7 1.7	1478 1505	95.4 97.1	52000	52000 56000	173 49	11.5	1351 1400	90.1 93.3
60000	64000	17	1.1	1522	98.2 99.0	56000 60000	60000 64000	49 27	3.3 1.8	1449 1476	96.6 98.4
64000 68000	68000 72000 76000	13 2 4	0.8	1535 1537	99.2	64000 68000	68000 72000	9 5	0.6	1485 1490	99.0
72000 76000 80000	80000	5 4	0.3 0.3 0.3	1541 1546 1550	99.4 99.7 100.0	72000 76000	76000 80000	1 4	0.1 0.3	1491 1495	99.4 99.7
TOTAL	84000	1550	100.0	1000	100.0	80000 TOTAL	84000	5 1500	0.3	1500	100.0

						STATIST	IX FOR W	INDOWS	August		
\$TATISTIX	FOR SUM	FLOW	Jaly			FREQUEN	CY DISTR	IBUTION			
FREQUENCY DISTRIBUTION OF SUMFLOW CUMULATIVE											
12000 16000 20000 24000 28000 32000 40000 44000 44000 52000 60000 64000 68000 72000	HIGH 12000 16000 24000 24000 32000 32000 32000 40000 44000 48000 56000 66000 664000 68000 772000 84000 84000	FREQ F 4 4 4 17 44 100 143 144 175 2063 173 145 72 40 16 11 13 1550	PERCENT 0.5 0.3 1.1 2.8 6.5 9.2 9.3 11.3 13.0 10.2 9.4 4.6 4.9 2.6 1.0 0.8 100.0		LATIVE PERCENT 0.8 1.0 2.1 5.0 11.4 20.6 29.9 41.2 54.3 64.8 75.9 85.3 89.9 94.8 97.4 98.5 99.2	LOW 10000 12000 12000 12000 12000 18000 20000 22000 24000 36000 36000 36000 36000 440000 440000 48000 50000 52000 5500000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 550000 5500000 550000 550000 550000 550000 550000 550000 550000 550000 5500000 550000 550000 550000 550000 550000 550000 550000 550000 5500000 550000 550000 550000 550000 550000 550000 550000 550000 5500000 550000 550000 550000 550000 550000 550000 550000 550000 55000000	12000 14000 18000 20000 22000 24000 25000 34000 34000 34000 42000 42000 44000 46000 46000 56000 56000 56000 56000	FREQ 3 3 1 1 1 5 5 3 6 1 6 1 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7	0.2 0.1 0.3 0.3 0.0 1.5 5.7 7.3 5.8 5.8 5.9 7.9 11.4 7.8 4.5 3.2	77 77 13 16 32 56 173 261 173 261 274 452 542 634 746 923 1068 1190 1295 1364 1417 1447 1448 150	
			Septem	her.		60000 62000	62000	34	0.4	1542 1548	99.5 99.9
STATISTI				70.754		64000 TOTAL	66000	2 1550	0.1 100.0	1550	100.0
FREQUENC'	Y DISTRIE	BUTION O	F SUMFLOW								
LOW 20000 22000 24000	HIGH 22000 24000 26000	FREQ 5 15 25	PERCENT 0.3 1.0 1.7	CUMI FREQ 5 20 45	JLATIVE PERCENT 0.3 1.3 3.0		× FOR WI		October OF SUMFLOW		
26000 28000 30000 32000 34000 36000	28000 30000 32000 34000 36000 38000	37 68 68 106 154 142	2.5 4.5 4.5 7.1 10.3 9.5	82 150 218 324 478 620	5.5 10.0 14.5 21.6 31.9 41.3	LOW 6000 8000 10000	HIGH 8000 10000 12000	FREQ 1 2 1	PERCENT 0.1 0.1 0.1	FREQ 1 3 4	JLATIVE PERCENT 0.1 0.2 0.3
38000 40000 42000 44000 46000 48000 50000 52000	40000 42000 44000 46000 48000 50000 52000 54000	136 185 129 98 108 65 26 15	9.1 12.3 8.6 6.5 7.2 4.3 1.7	756 941 1070 1168 1276 1341 1367 1382	50.4 62.7 71.3 77.9 85.1 89.4 91.1 92.1	12000 14000 16000 18000 20000 22000 24000 26000	14000 16000 18000 20000 22000 24000 26000 28000	1 5 13 50 31 79 97	0.1 0.3 0.8 3.2 2.0 5.1 6.3	5 6 11 24 74 105 184 281	0.3 0.4 0.7 1.5 4.8 6.8 11.9
54000 56000 58000 60000 62000 64000 66000 TOTAL	56000 58000 60000 62000 64000 66000 68000	27 23 22 18 15 8 5	1.8 1.5 1.5 1.2 1.0 0.5 0.3	1409 1432 1454 1472 1487 1495 1500	93.9 95.5 96.9 98.1 99.1 99.7 100.0	28000 30000 32000 34000 36000 38000 40000 42000	30000 32000 34000 36000 38000 40000 42000 44000	107 147 209 167 140 127 144	6.9 9.5 13.5 10.8 9.0 8.2 9.3 6.4	388 535 744 911 1051 1178 1322 1421	25.0 34.5 48.0 58.8 67.8 76.0 85.3 91.7
						44000 46000 48000 50000	46000 48000 50000 52000	60 34 13 8	3.9 2.2 0.8 0.5	1481 1515 1528 1536	95.5 97.7 98.6 99.1
	IX FOR W		Nevem of sumfloy			52000 54000 TOTAL	54000 56000	8 6 1550	0.5 0.4 100.0	1544 1550	99.6 100.0
LOW 4000 6000	6000 8000	FREQ 2 6	PERCENT 0.1 0.4	FREQ 2 8	MULATIVE PERCENT 0.1 0.5	STATISTIX FREQUENCY			Decemb	er	
8000 10000		21 51	1.4 3.4	29 80	1.9 5.3	i integotine i	DIDIKID	0,10,	OPII LON	CUMU	LATIVE
12000 14000 16000 18000 20000	16000 18000 20000 22000	98 100 116 171 187	6.5 6.7 7.7 11.4 12.5	178 278 394 565 752	11.9 18.5 26.3 37.7 50.1	6000 8000	HIGH 8000 10000 12000 14000	FREQ 41 84 218 382	PERCENT 2.6 5.4 14.1 24.6		PERCENT 2.6 8.1 22.1 46.8
22000 24000 26000 28000 30000 32000 34000	26000 28000 30000 32000 34000 36000	155 166 128 90 70 54 38 37	10.3 11.1 8.5 6.0 4.7 3.6 2.5 2.5	907 1073 1201 1291 1361 1415 1453	60.5 71.5 80.1 86.1 90.7 94.3 96.9 99.3	16000 18000 20000 22000 24000 26000	16000 18000 20000 22000 24000 26000 28000	299 188 118 69 47 41	19.3 12.1 7.6 4.5 3.0 2.6 2.4	1024 1212 1330 1399 1446 1487 1524	66.1 78.2 85.8 90.3 93.3 95.9 98.3
38000 40000 TOTAL	40000	9 1 1500	0.6 0.1 100.0	1499 1500	99.9 100.0		30000 32000	18 8 1550	1.2 0.5 100.0	1542 1550	99.5 100.0