



Aalto-yliopisto  
Perustieteiden  
korkeakoulu

# Identifying Representative Weeks for the Finnish Power Sector with Time-Series Clustering

*Ilona Ylikoski*

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*Advisor: Afzal Siddiqui*

*Supervisor: Afzal Siddiqui*

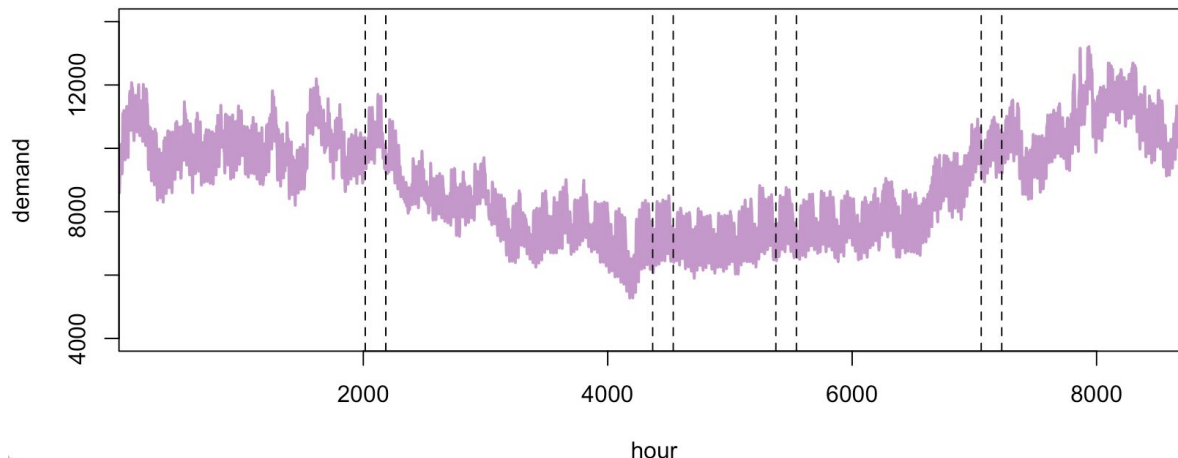
Työn saa tallentaa ja julkistaa Aalto-yliopiston avoimilla verkkosivuilla. Muilta osin kaikki oikeudet pidätetään.

# Background

- Power system models can be complex and computationally intractable problem instances
- To simplify the models, their temporal resolution can be reduced
  - Time series constraints can be simplified by using representative periods instead of full datasets.

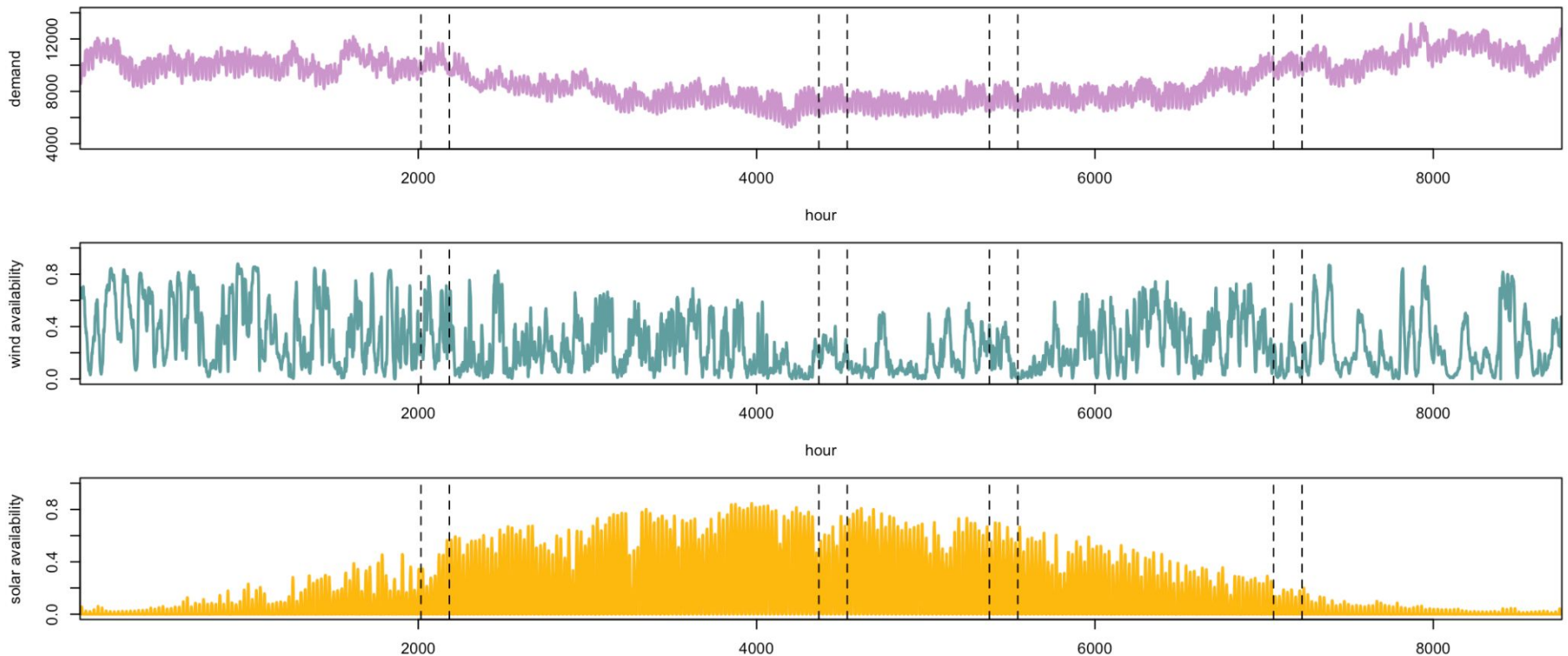
# Goals

- Apply time-series aggregation techniques to Finnish demand, wind and solar data.
- Compare the results of two different approaches to aggregate data into four representative weeks
  1. Partitional approach
  2. Seasonal approach



# Data

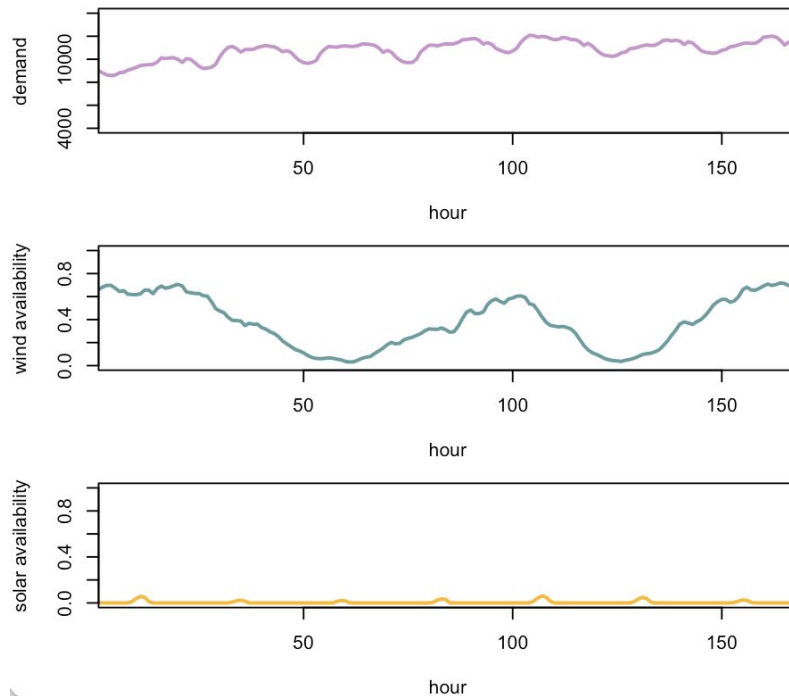
- Hourly time-series for consumption [1] as well as wind [2], and solar [3] availability for 2023



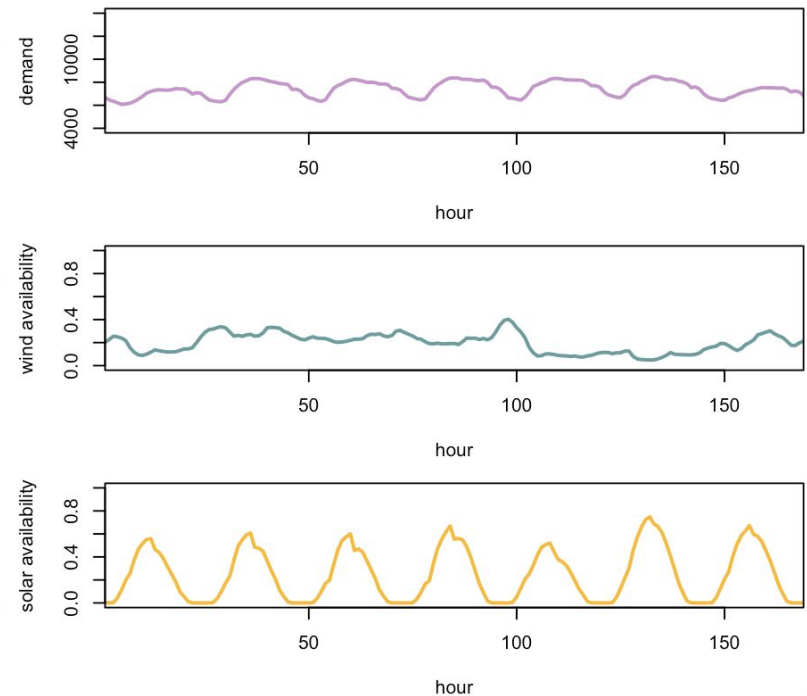
# Data

- Data are split into 52 168-hour weeks
- The last day is represented by the first 24 hours of the previous week

Week 1



Week 26



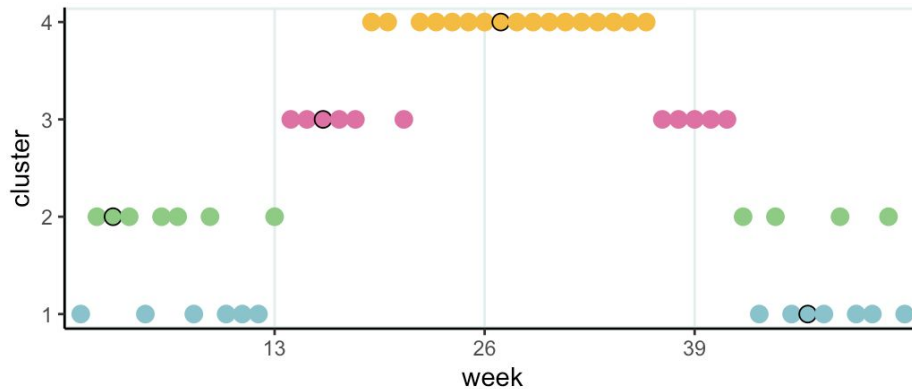
# The Two Approaches

- Two different aggregation approaches for the data were compared
- Partitional approach
  - Use a clustering algorithm to determine groups in the data.
  - Choose a representative week as the medoid of each cluster.
- Seasonal approach
  - Take predetermined groups in data
  - Choose representative weeks in terms of a test statistic

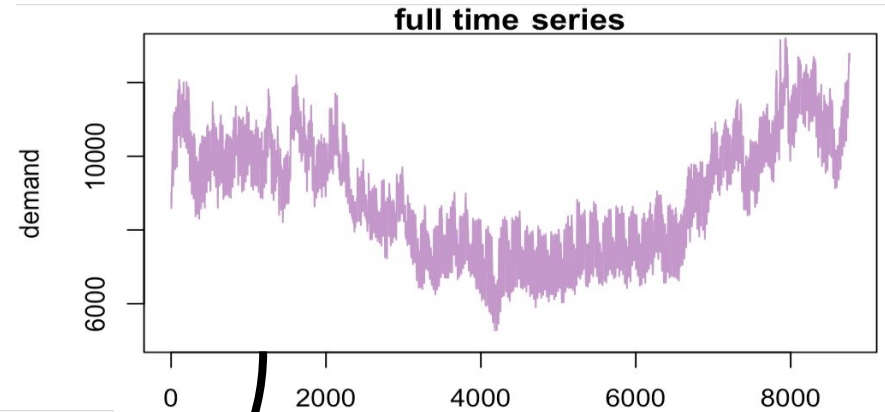
# Partitional Approach

The clustering algorithm assigns each week to a cluster

clustering result



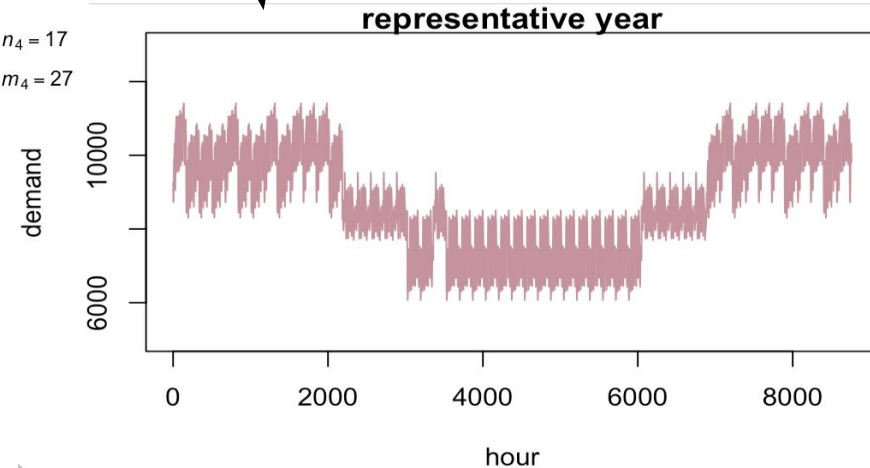
each week  $w$  is represented by the medoid  $m_c$  of the cluster  $c$  it is assigned to



- $n_1 = 13$   
 $m_1 = 46$
- $n_2 = 11$   
 $m_2 = 3$
- $n_3 = 11$   
 $m_3 = 16$
- $n_4 = 17$   
 $m_4 = 27$

distances between pairs of normalised weeks are computed

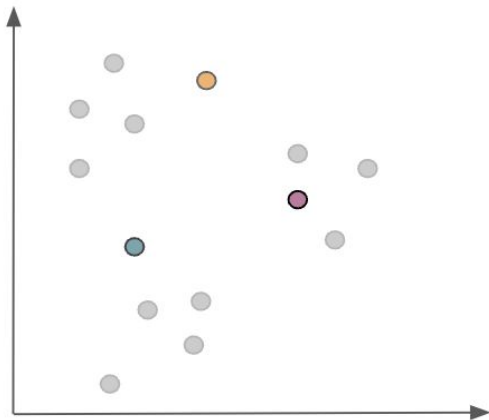
a representative year is formed for each variable



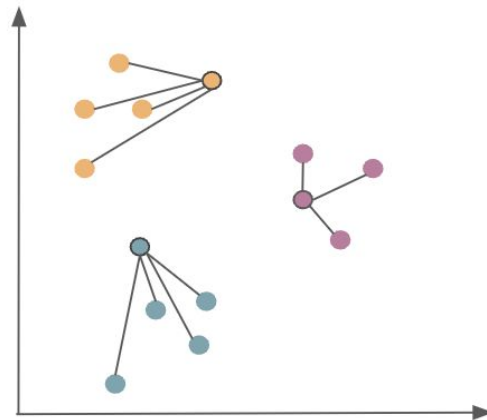
# Partitioning Around Medoids (PAM)

- Partitional clustering algorithm, implemented with R-package “cluster” [4]
- Chosen because
  1. Medoids are real objects (weeks) and can be directly chosen as the representative weeks
  2. Greedy selection of starting points leads to semi-deterministic outcomes.

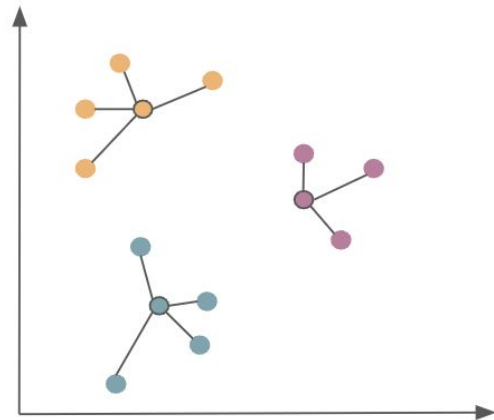
1. Greedy selection of initial medoids



2. Assign each remaining object to its nearest medoid



3. Swap medoids until total sum distances cannot be further minimised





# Measuring Dissimilarity of Weeks

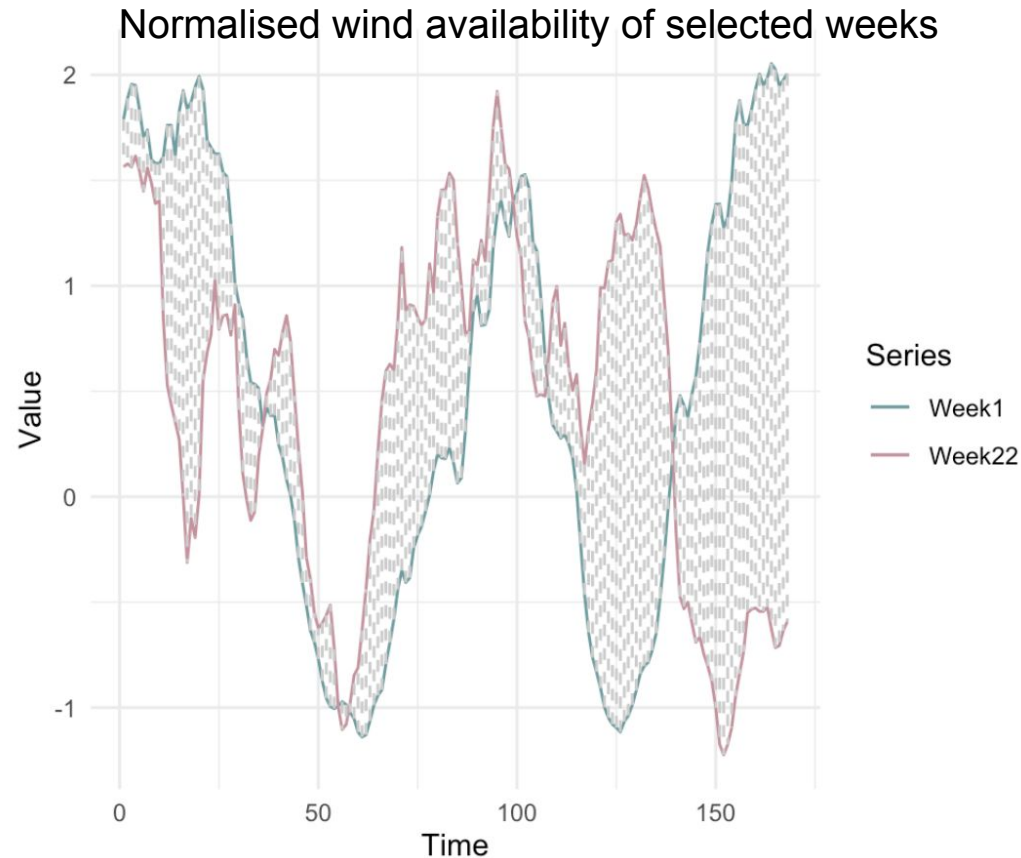
- Each time step  $t$  of week  $x$  is compared to the same time step of week  $y$ .
- L2 = Euclidean distance

$$d_{L2}(\bar{x}, \bar{y}) = \sqrt{\sum_{t \in T} (x_t - y_t)^2}$$

- L1 = Manhattan distance

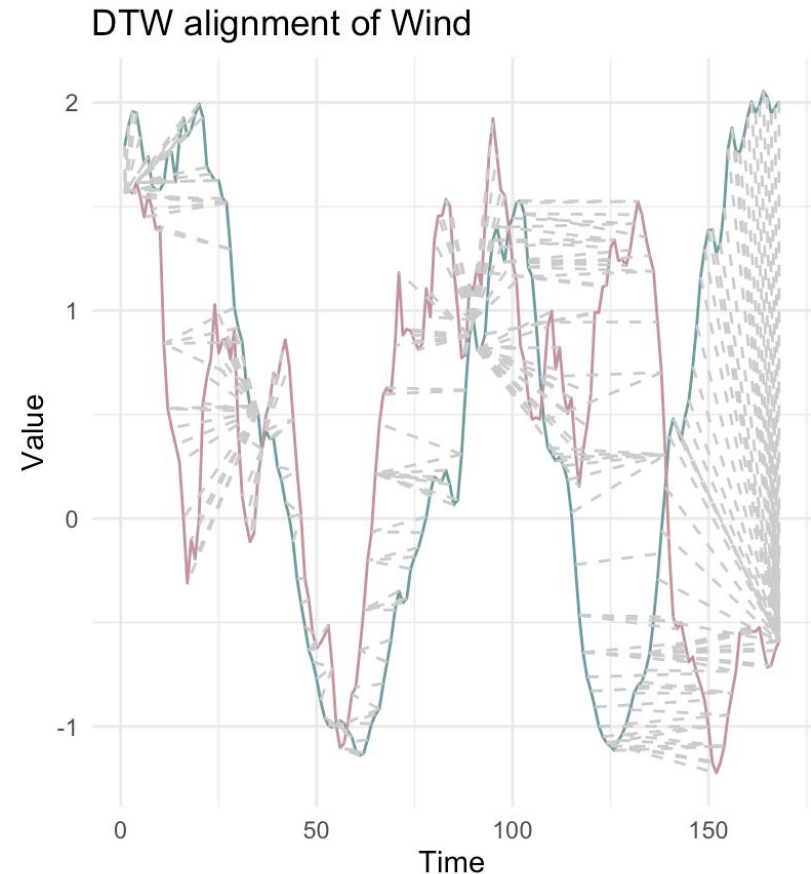
$$d_{L1}(\bar{x}, \bar{y}) = \sum_{t \in T} |x_t - y_t|$$

$$T = \{Z \cap [1, 168]\}$$



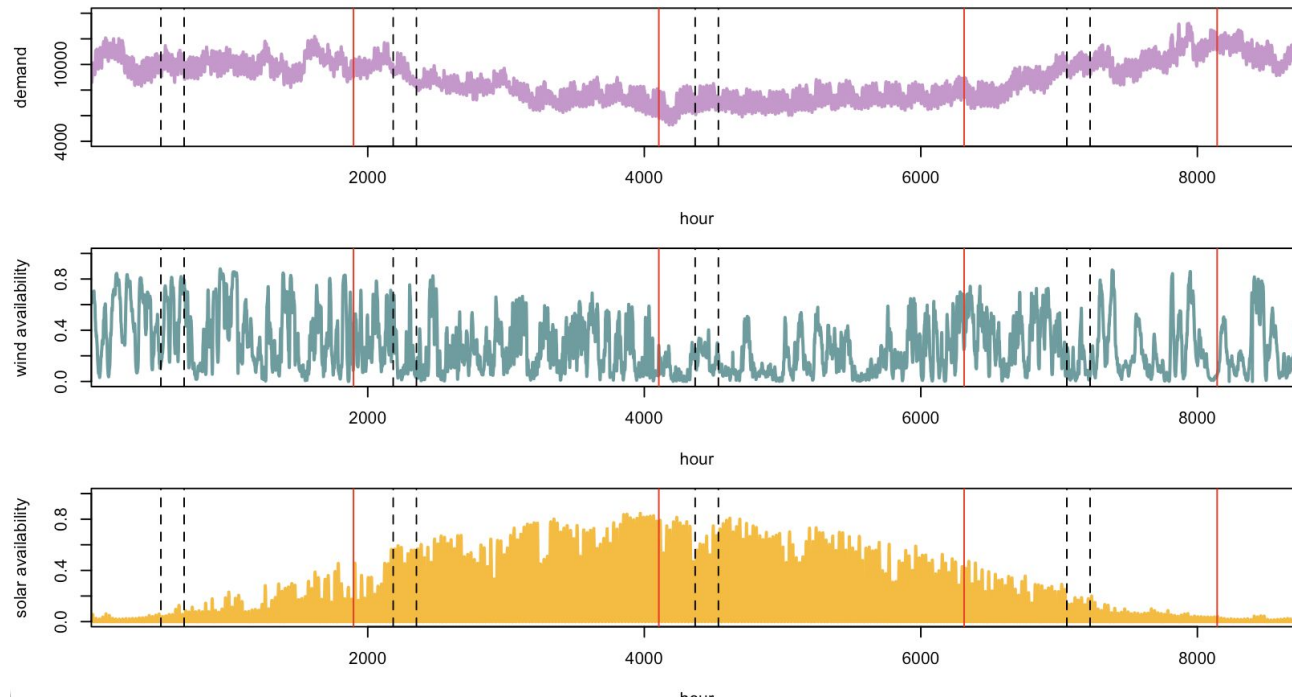
# Alignments

- In addition to pointwise comparison of time steps, Dynamic Time Warping (DTW) is also considered
  - Implemented with R-package “dtw” [5]
- Wind production is very stochastic
  - The peaks in generation do not necessarily align like for demand and solar
- Tests were done both with and without a constraint on how far time can be warped
  - Itakura parallelogram defines a window for time warping [5]



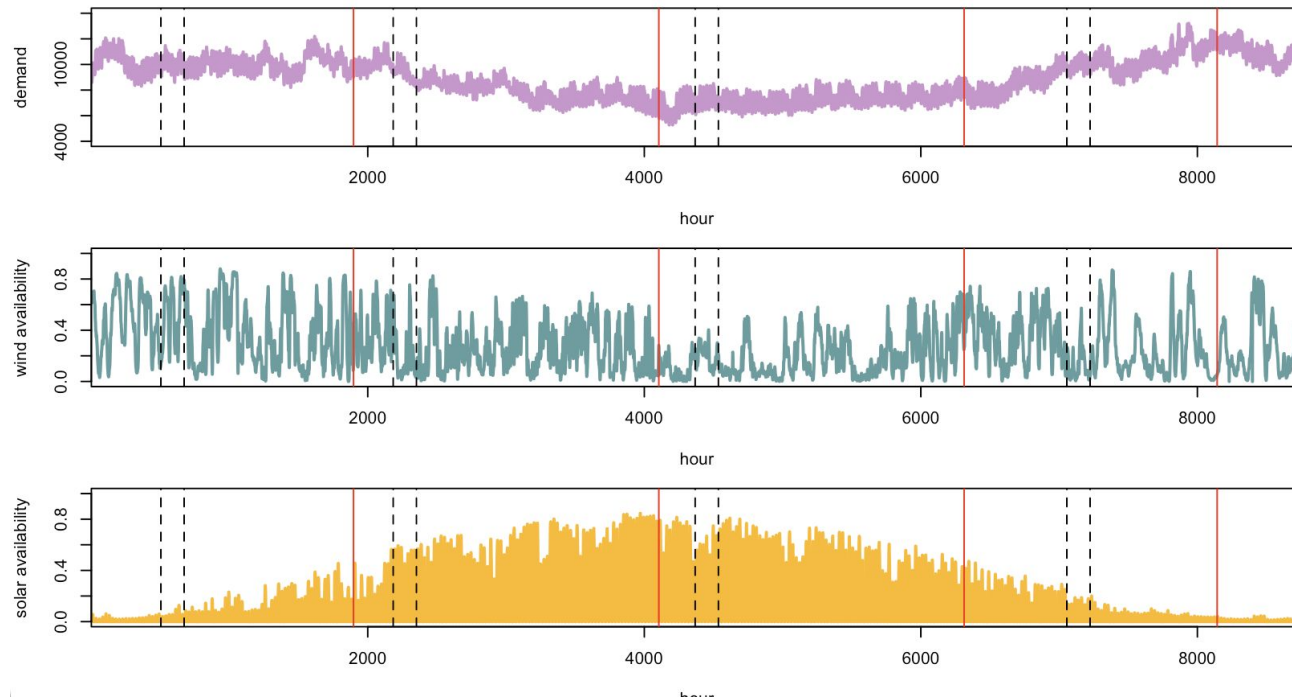
# Seasonal Approach

- Representative weeks are chosen from predetermined equal-sized seasons
- Implemented with a modified version of the GAMS script used in [6]



# Seasonal Approach

- Minimising the seasonal-weekly error in (1) the mean and (2) the standard error within each season
  - i.e. finding the week within each season that has mean and s.e. closest to the average over the whole season



# Measuring Representativity

- Benchmark optimisation model
  - A capacity expansion model for Finland the year 2023
    - Modified from [6] and [7]
    - Implemented in GAMS
  - Minimise annual cost of operations, generation, and possible investment
    - Wind, solar and hydro generation has zero cost
    - Cost of thermal generation determined by fuel
  - Hydro reservoir creates dependency across time steps
- Selected statistical values representing the mean and the variance in the time series

# Measuring Representativity

- Quality of representative weeks is analysed based on the error in selected statistics
  - Benchmark model - comparison to FTR
    - obj = Objective function value of benchmark model
    - W% = Share of total demand generated with wind power
  - Demand
    - $\mu_Q$  = Mean of hourly demand
    - $s_Q$  = Standard deviation of demand
  - Wind
    - $\mu_W$  = Mean of hourly wind availability
    - $s_W$  = Standard deviation of wind availability

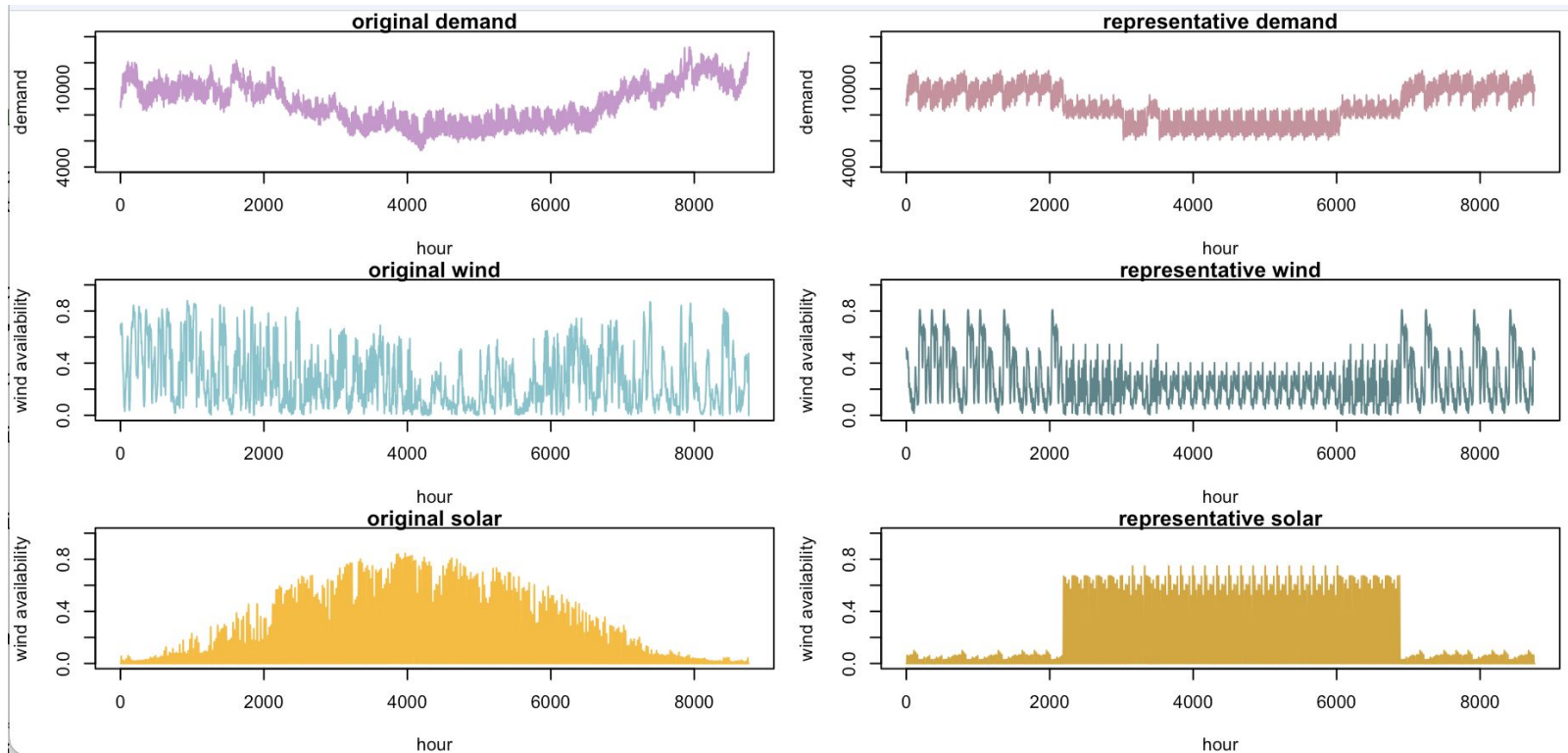
# Results with the Partitional Approach

Wind + Demand	obj	W%	$\mu_Q$	$s_Q$	$\mu_W$	$s_W$
L2	-2,54 %	-8,12 %	-1,31 %	-7,37 %	-9,39 %	-20,47 %
L1	-0,78 %	-11,05 %	0,33 %	-2,46 %	-11,55 %	-26,51 %
DTW L1	-5,34 %	-1,61 %	-0,74 %	-0,74 %	-3,25 %	-13,95 %
DTW L1 window	-2,38 %	-6,81 %	1,12 %	-10,68 %	-6,86 %	-18,60 %
DTW L2	-5,72 %	-2,16 %	-1,09 %	-1,50 %	-4,33 %	-14,88 %
DTW L2 window	-2,07 %	-6,81 %	1,12 %	-10,68 %	-6,86 %	-18,60 %

- Objective function value lower than FTR for all variants
  - Likely due to lower share of outlier hours in representative weeks than in the original time series

# Results with L2 Distance

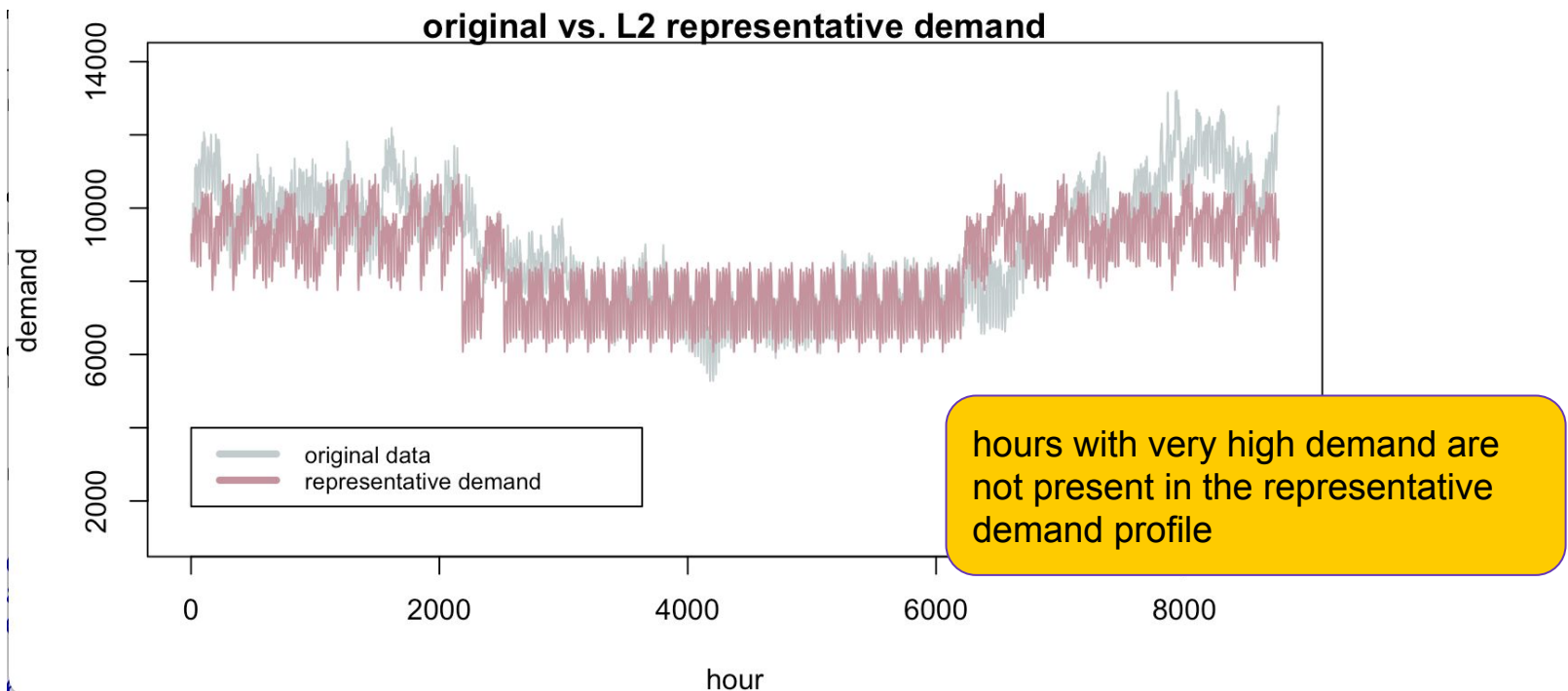
Wind + Demand	obj	W%	$\mu_Q$	$S_Q$	$\mu_W$	$S_W$
L2	-2,54 %	-8,12 %	-1,31 %	-7,37 %	-9,39 %	-20,47 %





# Results with L2 distance

Wind + Demand	obj	W%	$\mu_Q$	$s_Q$	$\mu_W$	$s_W$
L2	-2,54 %	-8,12 %	-1,31 %	-7,37 %	-9,39 %	-20,47 %

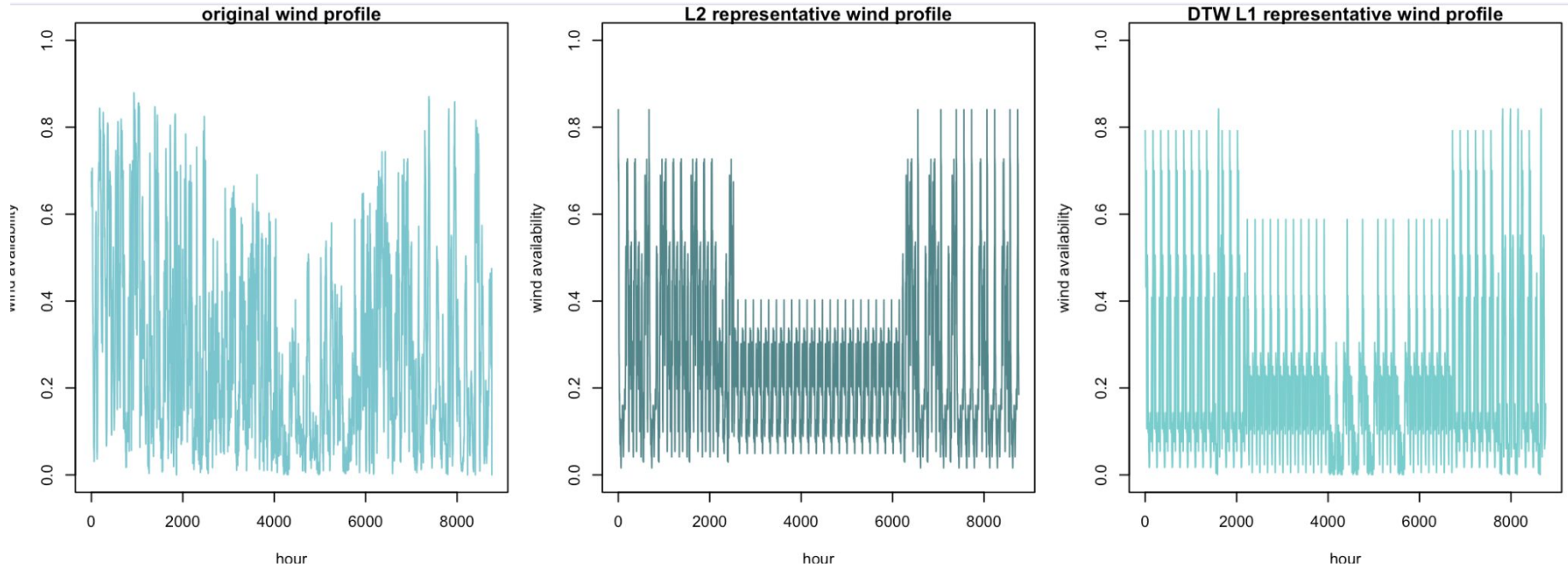


# Results with the Partitional Approach

Wind + Demand	obj	W%	$\mu_Q$	$s_Q$	$\mu_W$	$s_W$
L2	-2,54 %	-8,12 %	-1,31 %	-7,37 %	-9,39 %	-20,47 %
L1	-0,78 %	-11,05 %	0,33 %	-2,46 %	-11,55 %	-26,51 %
DTW L1	-5,34 %	-1,61 %	-0,74 %	-0,74 %	-3,25 %	-13,95 %
DTW L1 window	-2,38 %	-6,81 %	1,12 %	-10,68 %	-6,86 %	-18,60 %
DTW L2	-5,72 %	-2,16 %	-1,09 %	-1,50 %	-4,33 %	-14,88 %
DTW L2 window	-2,07 %	-6,81 %	1,12 %	-10,68 %	-6,86 %	-18,60 %

- Mean demand tracked well with all variants
  - Standard deviation however is lower
- Wind mean and generation lower than expected
  - DTW alignments perform better in this regard

# Representative Wind Profiles



Wind + Demand	obj	W%	$\mu_Q$	$S_Q$	$\mu_W$	$S_W$
L2	-2,54 %	-8,12 %	-1,31 %	-7,37 %	-9,39 %	-20,47 %
DTW L1	-5,34 %	-1,61 %	-0,74 %	-0,74 %	-3,25 %	-13,95 %

# Results with the Partitional Approach

Wind + Demand + Solar	obj	W%	$\mu_Q$	$s_Q$	$\mu_W$	$s_W$
L2	-4,37 %	-2,31 %	-2,49 %	-5,65 %	-5,05 %	-15,81 %
L1	-1,80 %	-8,61 %	-0,49 %	-5,01 %	-9,03 %	-14,42 %
DTW L1	-1,96 %	-0,59 %	-0,66 %	-2,38 %	-2,17 %	-1,40 %
DTW L1 window	-3,03 %	-0,67 %	-1,28 %	-3,87 %	-2,89 %	-13,02 %
DTW L2	-0,33 %	-11,93 %	-0,98 %	-2,63 %	-13,72 %	-6,98 %
DTW L2 window	-3,03 %	-0,67 %	-1,28 %	-3,87 %	-2,89 %	-13,02 %

- After adding solar
  - Error in the objective function value decreases with the unconstrained DTW alignments and increases with the others

# Results with the Seasonal Approach

- Performs well in terms of the variable means
  - Expected as it is directly in the minimised objective criteria
- However, the error in the objective function value is higher
  - Likely due to the lower obtained variance in the demand
  - Adding a higher weight to consumption (Q) leads to some improvement

Variables	obj	W%	$\mu_Q$	$s_Q$	$\mu_W$	$s_W$
Equal weights (WQ, WQS)	-8,14 %	+0,44 %	-0,14 %	-30,40 %	-0,72 %	-2,79 %
1,5xQ, 2xQ and 1xW (WQ)	-3,72%	+0,26%	-1,10%	-12,28%	-1,08%	-5,58%

# Conclusions

- No one method clearly outperformed the others
- Both approaches dampen outliers
  - Reflected in the lower objective function values than the FTR
  - Number of representative weeks was fixed at four, which likely aggravated the effect
- Low error in the mean and standard deviation did not guarantee low error in the objective function or vice versa

# References

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